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**zip** — Zero-inflated Poisson regression

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# **Description**

zip fits a zero-inflated Poisson (ZIP) model to count data with excess zero counts. The ZIP model assumes that the excess zero counts come from a logit or probit model and the remaining counts come from a Poisson model.

### **Quick start**

Zero-inflated Poisson model of y on x1 and x2 with inflation modeled using x3 zip y x1 x2, inflate(x3)

Use a probit model instead of a logit model to predict excess zeros zip y x1 x2, inflate(x3) probit

### Menu

Statistics > Count outcomes > Zero-inflated Poisson regression

### **Syntax**

```
zip depvar [indepvars] [if] [in] [weight],
    inflate(varlist[, offset(varname)]|_cons) [options]
```

options	Description				
Model					
* <u>inf</u> late()	equation that determines whether the count is zero				
<u>nocons</u> tant	suppress constant term				
$exposure(varname_e)$	include $ln(varname_e)$ in model with coefficient constrained to 1				
$\underline{off}set(\mathit{varname}_o)$	include $varname_o$ in model with coefficient constrained to 1				
<pre>constraints(constraints)</pre>	apply specified linear constraints				
probit	use probit model to characterize excess zeros; default is logit				
SE/Robust					
vce(vcetype)					
Reporting					
<u>l</u> evel(#)	set confidence level; default is level(95)				
irr	report incidence-rate ratios				
<u>nocnsr</u> eport	do not display constraints				
display_options	control columns and column formats, row spacing, line width, display of omitted variables and base and empty cells, and factor-variable labeling				
Maximization					
maximize_options	control the maximization process; seldom used				
<u>col</u> linear	keep collinear variables				
<u>coefl</u> egend	display legend instead of statistics				
	1.				

<sup>\*</sup> $\frac{\text{inf}}{\text{late}(varlist}$ ,  $\frac{\text{off}}{\text{set}(varname)}$ ] | \_cons) is required.

indepvars and varlist may contain factor variables; see [U] 11.4.3 Factor variables.

bayes, bootstrap, by, collect, fp, jackknife, rolling, statsby, and svy are allowed; see [U] 11.1.10 Prefix commands. For more details, see [BAYES] bayes: zip.

Weights are not allowed with the bootstrap prefix; see [R] bootstrap.

vce() and weights are not allowed with the svy prefix; see [SVY] svy.

fweights, iweights, and pweights are allowed; see [U] 11.1.6 weight.

collinear and coeflegend do not appear in the dialog box.

See [U] 20 Estimation and postestimation commands for more capabilities of estimation commands.

### **Options**

```
Model
```

inflate(varlist[, offset(varname)] | \_cons) specifies the equation that determines whether the
 observed count is zero. Conceptually, omitting inflate() would be equivalent to fitting the model
 with poisson; see [R] poisson.

inflate(varlist[, offset(varname)]) specifies the variables in the equation. You may optionally include an offset for this *varlist*.

inflate(\_cons) specifies that the equation determining whether the count is zero contains only an intercept. To run a zero-inflated model of *depvar* with only an intercept in both equations, type zip *depvar*, inflate(\_cons).

noconstant, exposure  $(varname_e)$ , offset  $(varname_o)$ , constraints (constraints); see [R] Estimation options.

probit requests that a probit, instead of logit, model be used to characterize the excess zeros in the data.

SE/Robust

vce(vcetype) specifies the type of standard error reported, which includes types that are derived from asymptotic theory (oim, opg), that are robust to some kinds of misspecification (robust), that allow for intragroup correlation (cluster clustvar), and that use bootstrap or jackknife methods (bootstrap, jackknife); see [R] vce\_option.

Reporting

level(#); see [R] Estimation options.

irr reports estimated coefficients transformed to incidence-rate ratios, that is,  $e^b$  rather than b. Standard errors and confidence intervals are similarly transformed. This option affects how results are displayed, not how they are estimated or stored. irr may be specified at estimation or when replaying previously estimated results.

nocnsreport; see [R] Estimation options.

display\_options: noci, nopvalues, noomitted, vsquish, noemptycells, baselevels,
 allbaselevels, nofvlabel, fvwrap(#), fvwrapon(style), cformat(%fmt), pformat(%fmt),
 sformat(%fmt), and nolstretch; see [R] Estimation options.

Maximization

maximize\_options: difficult, technique(algorithm\_spec), iterate(#), [no]log, trace,
 gradient, showstep, hessian, showtolerance, tolerance(#), ltolerance(#),
 nrtolerance(#), nonrtolerance, and from(init\_specs); see [R] Maximize. These options are
 seldom used.

Setting the optimization type to technique (bhhh) resets the default *vcetype* to vce(opg).

The following options are available with zip but are not shown in the dialog box: collinear, coeflegend; see [R] Estimation options.

## Remarks and examples

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Zero-inflated Poisson (ZIP) models address the case when the data contain a higher fraction of zeros than is likely to be generated from a Poisson model. Having a large proportion of zero observations, in itself, does not necessarily mean that we have the excess zeros problem. For instance, a Poisson model with a mean value of 0.2 predicts that  $P(Y=0)=\exp(-0.2)\approx 0.82$ . However, the range of possible outcomes is restricted because of the small variance, 0.2 (mean and variance are equal for a Poisson model), as shown by  $P(Y>3)\approx 0.00006$ . Unlike Poisson models, ZIP models allow us to have a large fraction of zeros without restricting the range of outcomes.

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ZIP models assume that an observation is 0 with a probability p or is a realization of a Poisson random variable, which can also be 0, with a probability 1-p. For instance, you might count how many fish each visitor to a park catches. Many visitors may catch zero, because they do not fish (as opposed to being unsuccessful). Using a logit or probit model, you may model the probability p of whether a person does not fish depending on several covariates related to fishing. Using a Poisson distribution, you may model how many fish a person catches depending on several covariates having to do with the success of catching fish (type of lure or bait, time of day, temperature, season, etc.). This is the type of data for which the zip command is useful.

See Long (1997, 242–247) and Cameron and Trivedi (2005, 680–681) for a discussion of the ZIP model and other zero-modified count models.

#### Example 1: Fitting a ZIP model

We have fictional data on the number of fish caught (count) by visitors to a national park on a particular day. Some of the visitors do not fish, but we do not have the data on whether a person fished; we merely have data on how many fish were caught together with several covariates.

Variable count exhibits an excess of zero observations (142 of 250 observations), beyond what would be expected from a Poisson model. We suspect that the number of zeros may be inflated because many visitors are not fishing. That is, a zero observation may be the result of a visitor who was unfortunate and caught no fish but may also be because the visitor did not fish. A standard Poisson model (see [R] **poisson**) treats these two types of zero observations as a homogeneous group, which typically leads to biased statistical results. We would like to distinguish between the two types of zeros and possibly draw inference for them separately (see example 1 in [R] **zip postestimation**).

The zip command allows us to model the two types of zeros. First, using the required option inflate(), we model whether a visitor fishes as a function of the number of children accompanying him or her (child) and whether he or she is camping (camper). Next, we assume the response variable, count, depends on whether the visitor used a live bait (livebait) and the number of persons (persons), which includes the visitor and any adults or children accompanying him. Note that persons is always greater than child.

```
. use https://www.stata-press.com/data/r18/fish
(Fictional fishing data)
. zip count persons livebait, inflate(child camper)
Fitting constant-only model:
Iteration 0: Log likelihood = -1347.807
              Log likelihood = -1305.3245
Iteration 1:
Iteration 2:
              Log likelihood = -1104.3005
Iteration 3:
              Log likelihood = -1103.9426
Iteration 4: Log likelihood = -1103.9425
Fitting full model:
Iteration 0:
              Log likelihood = -1103.9425
Iteration 1:
              Log likelihood = -896.2346
Iteration 2:
              Log likelihood = -851.61723
Iteration 3:
              Log likelihood = -850.70435
Iteration 4:
              Log likelihood = -850.70142
Iteration 5:
              Log likelihood = -850.70142
Zero-inflated Poisson regression
                                                         Number of obs =
                                                                             250
Inflation model: logit
                                                         Nonzero obs
                                                                             108
                                                                             142
                                                         Zero obs
                                                         LR chi2(2)
                                                                       = 506.48
Log likelihood = -850.7014
                                                         Prob > chi2
                                                                       = 0.0000
       count
               Coefficient
                            Std. err.
                                            z
                                                 P>|z|
                                                            [95% conf. interval]
count
                 .8068853
                             .0453288
                                                 0.000
                                                            .7180424
                                                                        .8957281
     persons
                                         17.80
    livebait
                 1.757289
                             .2446082
                                          7.18
                                                 0.000
                                                           1.277866
                                                                       2.236713
                -2.178472
                             .2860289
                                         -7.62
                                                 0.000
                                                          -2.739078
                                                                      -1.617865
       _cons
inflate
```

Coefficients in the upper half of the table correspond to the Poisson model for individuals who fished. For instance, among visitors who fished, using a live bait increases the expected number of caught fish by a factor of  $\exp(1.7572) \approx 5.8$ , holding other covariates constant.

5.73

-2.78

-1.58

0.000

0.005

0.114

1.054228

-1.731593

-1.10273

2.150913

-.2998038

.1181558

4

.2797719

.365259

.3114562

1.602571

-1.015698

-.4922872

### Example 2: Comparing model fit

child

\_cons

camper

When you have count data, you may want to test whether a conventional count data model or a zero-inflated count data model is preferable. The classical likelihood-ratio test cannot be used here because the models are not nested. But we can use information criteria such as the AIC and BIC to check whether the standard or zero-inflated model is more appropriate.

Continuing with our fishing example, let's check whether the standard Poisson or ZIP model is more appropriate for our data. First, we store the estimation results from the previous ZIP model by typing

. estimates store zip

Next, we fit the Poisson model corresponding to the main equation of the ZIP model and store its results as pois:

- . poisson count persons livebait
   (output omitted)
- . estimates store pois

We use estimates stats to display the AIC and BIC values for the two models.

. estimates stats pois zip

Akaike's information criterion and Bayesian information criterion

Model	N	11(null)	ll(model)	df	AIC	BIC
pois zip		-1647.716 -1103.942		3 6	2630.356 1713.403	2640.92 1734.532

Note: BIC uses N = number of observations. See [R] IC note.

The ZIP model has smaller AIC and BIC values; we thus conclude that it fits our data better than the standard Poisson model.

### Stored results

zip stores the following in e():

```
Scalars
    e(N)
                              number of observations
                              number of zero observations
    e(N_zero)
                              number of parameters
    e(k)
                              number of equations in e(b)
    e(k_eq)
    e(k_eq_model)
                              number of equations in overall model test
    e(k_dv)
                              number of dependent variables
    e(df_m)
                              model degrees of freedom
    e(11)
                              log likelihood
    e(11_0)
                              log likelihood, constant-only model
    e(N_clust)
                              number of clusters
    e(chi2)
                              \chi^2
    e(p)
                              p-value for model test
                              rank of e(V)
    e(rank)
    e(ic)
                              number of iterations
    e(rc)
                              return code
    e(converged)
                              1 if converged, 0 otherwise
Macros
    e(cmd)
                              zip
                              command as typed
    e(cmdline)
                              name of dependent variable
    e(depvar)
                              logit or probit
    e(inflate)
    e(wtype)
                              weight type
    e(wexp)
                              weight expression
    e(title)
                              title in estimation output
    e(clustvar)
                              name of cluster variable
                              offset
    e(offset1)
    e(offset2)
                              offset for inflate()
                              Wald or LR; type of model \chi^2 test
    e(chi2type)
    e(vce)
                              vcetype specified in vce()
    e(vcetype)
                              title used to label Std. err.
    e(opt)
                              type of optimization
```

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```
e(which)
                             max or min; whether optimizer is to perform maximization or minimization
    e(ml_method)
                             type of ml method
    e(user)
                             name of likelihood-evaluator program
    e(technique)
                             maximization technique
    e(properties)
    e(predict)
                             program used to implement predict
    e(asbalanced)
                             factor variables fyset as asbalanced
    e(asobserved)
                             factor variables fyset as asobserved
Matrices
    e(b)
                             coefficient vector
    e(Cns)
                             constraints matrix
                             iteration log (up to 20 iterations)
    e(ilog)
    e(gradient)
                             gradient vector
    e(V)
                             variance-covariance matrix of the estimators
    e(V_modelbased)
                             model-based variance
Functions
    e(sample)
                             marks estimation sample
```

In addition to the above, the following is stored in r():

```
Matrices
r(table) matrix containing the coefficients with their standard errors, test statistics, p-values, and confidence intervals
```

Note that results stored in r() are updated when the command is replayed and will be replaced when any r-class command is run after the estimation command.

#### Methods and formulas

Consider the formulation of a zero-inflated model as presented in Lambert (1992). Define

$$\xi_{j}^{\beta} = \mathbf{x}_{j}\boldsymbol{\beta} + \text{offset}_{j}^{\beta}$$
  

$$\xi_{j}^{\gamma} = \mathbf{z}_{j}\boldsymbol{\gamma} + \text{offset}_{j}^{\gamma}$$
  

$$\lambda_{j} = \exp\left(\xi_{j}^{\beta}\right)$$
  

$$F_{j} = F\left(\xi_{j}^{\gamma}\right)$$

where  $F(\cdot)$  is the inverse of the logit function or, if the probit option was specified, the inverse of the probit function (or the standard normal cumulative distribution function). All subjects are assumed to be independent with the jth response determined as follows:

$$Y_j = 0$$
 with probability  $F_j$  
$$Y_i \sim \text{Poisson}(\lambda_j) \text{ with probability } 1 - F_j$$

In other words,

$$Pr(Y_j = 0 | \mathbf{x}_j, \mathbf{z}_j) = F_j + (1 - F_j) \exp(-\lambda_j)$$

$$Pr(Y_j = n | \mathbf{x}_j, \mathbf{z}_j) = (1 - F_j) \exp(-\lambda_j) \frac{\lambda_j^n}{n!} \quad \text{for } n = 1, 2, \dots$$

The zip command maximizes the log-likelihood lnL, defined by

$$\begin{split} \ln & L = \sum_{j \in S} w_j \ln \left\{ F_j + (1 - F_j) \exp(-\lambda_j) \right\} \\ & + \sum_{j \not \in S} w_j \left\{ \ln (1 - F_j) - \lambda_j + \xi_j y_j - \ln(y_j!) \right\} \end{split}$$

where  $w_i$  are the weights and S is the set of observations for which the observed outcome  $y_i = 0$ .

This command supports the Huber/White/sandwich estimator of the variance and its clustered version using vce(robust) and vce(cluster clustvar), respectively. See [P] \_robust, particularly Maximum likelihood estimators and Methods and formulas.

zip also supports estimation with survey data. For details on VCEs with survey data, see [SVY] Variance estimation.

#### References

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#### Also see

- [R] zip postestimation Postestimation tools for zip
- [R] **zinb** Zero-inflated negative binomial regression
- [R] **nbreg** Negative binomial regression
- [R] **poisson** Poisson regression
- [R] **tnbreg** Truncated negative binomial regression
- [R] **tpoisson** Truncated Poisson regression

[BAYES] bayes: zip — Bayesian zero-inflated Poisson regression

[SVY] **svy estimation** — Estimation commands for survey data

[XT] **xtpoisson** — Fixed-effects, random-effects, and population-averaged Poisson models

[U] 20 Estimation and postestimation commands

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